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**From Modula  
to Oberon  
and  
The Programming  
Language Oberon**

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# From Modula to Oberon

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## Abstract

The programming language Oberon is the result of a concentrated effort to increase the power of Modula-2 and simultaneously to reduce its complexity. Several features were eliminated, and a few were added in order to increase the expressive power and flexibility of the language. This paper describes and motivates the changes. The language is defined in a concise report.

## Introduction

The programming language Oberon evolved from a project whose goal was the design of a modern, flexible, and efficient operating system for a single-user workstation. A principal guideline was to concentrate on properties that are genuinely essential and - as a consequence - to omit ephemeral issues. It is the best way to keep a system in hand, to make it understandable, explicable, reliable, and efficiently implementable.

Initially, it was planned to express the system in Modula-2 [1], as that language supports the notion of modular design quite effectively, and because an operating system has to be designed in terms of separately compilable parts with conscientiously chosen interfaces. In fact, an operating system should be no more than a set of basic modules, and the design of an application must be considered as a goal-oriented extension of that basic set: Programming is always extending a given system.

Whereas modern languages, such as Modula, support the notion of extensibility in the procedural realm, the notion is less well established in the domain of data types. Modula in particular does not allow the definition of new data types as extensions of other, programmer-defined types in an adequate manner. An additional feature was called for, thereby giving rise to an *extension* of Modula.

The concept of the planned operating system also called for a highly dynamic, centralized storage management relying on the technique of garbage collection. Although Modula does not prevent the incorporation of a garbage collector in principle, its variant record feature constitutes a genuine obstacle. As the new facility for extending types would make the variant record feature superfluous, the removal of this stumbling block was a logical decision. This step, however, gave rise to a *restriction* (subset) of Modula.

It soon became clear that the rule to concentrate on the essential and to eliminate the inessential should not only be applied to the design of the new system, but equally stringently to the language in which the system is formulated. The application of the principle thus led from Modula to a new language. The adjective new, however, has to be understood in proper context: Oberon evolved from Modula by very few additions and several subtractions. In relying on evolution rather than revolution we remain in the tradition of a long development that led from Algol to Pascal, then to Modula-2, and eventually to Oberon. The common trait of these languages are their procedural rather than functional model, and the strict typing of data. More fundamental even is perhaps the idea of abstraction: the language must be defined in terms of mathematical, abstract concepts without reference to any computing mechanism. Only if a language satisfies this criterion,

can it be called "higher-level". No syntactic coating whatsoever can earn a language this attribute alone.

The definition of a language must be coherent and concise. This can only be achieved by a careful choice of the underlying abstractions and an appropriate structure combining them. The language manual must be reasonably short, avoiding the explanation of individual cases derivable from the general rules. The power of a formalism must not be measured by the length of its description. To the contrary, an overly lengthy definition is a sure symptom of inadequacy. In this respect, not complexity but simplicity must be the goal.

In spite of its brevity, a description must be complete. Completeness is to be achieved within the framework of the chosen abstractions. Limitations imposed by particular implementations do not belong to a language definition proper. Examples of such restrictions are the maximum values of numbers, rounding and truncation errors in arithmetic, and actions taken when a program violates the stated rules. It should not be necessary to supplement a language definition with a voluminous standards document to cover "unforeseen" cases.

But neither should a programming language be a mathematical theory only. It must be a practical tool. This imposes certain limits on the terseness of the formalism. Several features of Oberon are superfluous from a purely theoretical point of view. They are nevertheless retained for practical reasons, either for programmers' convenience or to allow for efficient code generation without the necessity of complex, "optimizing" pattern matching algorithms in compilers. Examples of such features are the presence of several forms of repetitive statements, and of standard procedures such as INC, DEC, and ODD. They complicate neither the language conceptually nor the compiler to any significant degree.

These underlying premises must be kept in mind when comparing Oberon with other languages. Neither the language nor its defining document reach the ideal; but Oberon approximates these goals much better than its predecessors.

A compiler for Oberon has been implemented for the NS32000 processor family and is embedded in the Oberon operating environment. The following data provide an estimate of the simplicity and efficiency of the implementation, and readers are encouraged to compare them with implementations of other languages. (Measurements with 10MHz NS 32032).

|                | length of source program<br>lines | length of compiled code<br>characters | length of compiled code<br>bytes | time of self-compilation<br>sec |
|----------------|-----------------------------------|---------------------------------------|----------------------------------|---------------------------------|
| Parser         | 1116                              | 36719                                 | 9928                             | 11.53                           |
| Scanner        | 346                               | 9863                                  | 3388                             | 3.80                            |
| Import/Export  | 514                               | 18386                                 | 4668                             | 5.25                            |
| Code generator | 1963                              | 65901                                 | 21636                            | 21.02                           |
| Total          | 3939                              | 130869                                | 39620                            | 41.60                           |

Subsequently, we present a brief introduction to Oberon assuming familiarity with Modula (or Pascal), concentrating on the added features and listing the eliminated ones. In order to be able "to start with a clean table", the latter are taken first.

## Features omitted from Modula

### Data types

*Variant records* are eliminated, because they constitute a genuine difficulty for the implementation of a reliable storage management system based on automatic garbage collection. The functionality of variant records is preserved by the introduction of extensible data types.

*Opaque types* cater to the concept of abstract data type and information hiding. They are eliminated as such, because again the concept is covered by the new facility of extended record types.

*Enumeration types* appear to be a simple enough feature to be uncontroversial. However, they defy extensibility over module boundaries. Either a facility to extend given enumeration types would have to be introduced, or they would have to be dropped. A reason in favour of the latter, radical solution was the observation that in a growing number of programs the indiscriminate use of enumerations had led to a pompous style that contributed not to program clarity but rather to verbosity. In connection with import and export, enumerations give rise to the exceptional rule that the import of a type identifier also causes the (automatic) import of all associated constant identifiers. This exceptional rule defies conceptual simplicity and causes unpleasant problems for the implementor.

*Subrange types* were introduced in Pascal (and adopted in Modula) for two reasons: (1) to indicate that a variable accepts a limited range of values of the base type and to allow a compiler to generate appropriate guards for assignments, and (2) to allow a compiler to allocate the minimal storage space needed to store values of the indicated subrange. This appeared desirable in connection with packed records. Very few implementations have taken advantage of this space saving facility, because the additional compiler complexity is very considerable. Reason 1 alone, however, did not appear to provide sufficient justification to retain the subrange facility in Oberon.

With the absence of enumeration and subrange types, the general possibility to define *set types* based on given element types appeared as redundant. Instead, a single, basic type SET is introduced, whose values are sets of integers from 0 to an implementation-defined maximum.

The basic type *CARDINAL* had been introduced in Modula-2 in order to allow address arithmetic with values from 0 to  $2^{16}$  on 16-bit computers. With the prevalence of 32-bit addresses in modern processors, the need for unsigned arithmetic has practically vanished, and therefore the type *CARDINAL* has been eliminated. With it, the bothersome incompatibilities of operands of types *CARDINAL* and *INTEGER* have disappeared.

The notion of a definable index type of arrays has also been abandoned: All indices are by default integers. Furthermore, the lower bound is fixed to 0; array declarations specify a number of elements (length) rather than a pair of bounds. This break with a long standing tradition since Algol 60 demonstrates the principle of eliminating the inessential most clearly. The specification of an arbitrary lower bound provides no expressive power at all, but it introduces a non-negligible amount of hidden, computational effort. (Only in the case of static declarations can it be delegated to the compiler).

## Modules and import/export rules

Experience with Modula over the last eight years has shown that *local modules* were rarely used. The additional complexity of the compiler required to handle them, and the additional complications in the visibility rules of the language definition appear not to justify local modules.

The *qualification* of an imported object's identifier  $x$  by the exporting module's name  $M$ , viz.  $M.x$ , can be circumvented in Modula by the use of the import clause `FROM M IMPORT x`. This facility has also been discarded. Experience in programming systems involving many modules has taught that the explicit qualification of each occurrence of  $x$  is actually preferable. A simplification of the compiler is a welcome side-effect.

The dual role of the main module in Modula is conceptually confusing. It constitutes a *module* in the sense of a package of data and procedures enclosed by a scope of visibility, and at the same time it constitutes a single *procedure* called main program. Within the Oberon system, the notion of a main program has vanished. Instead, the system allows the user to activate any (exported, parameterless) procedure (called a command). Hence, the language excludes modules without explicit definition part, and every module is defined in terms of a definition part and an implementation part (*not definition module* and *implementation module*).

## Statements

The *with statement* has been discarded. Like in the case of imported identifiers, the explicit qualification of field identifiers is to be preferred.

The elimination of the *for statement* constitutes a break with another long standing tradition. The baroque mechanism of Algol 60's *for statement* had been trimmed significantly in Pascal (and Modula). Its marginal value in practice has led to its absence in Oberon.

## Low-level facilities

Modula-2 makes access to machine-specific facilities possible through low-level constructs, such as the data types ADDRESS and WORD, absolute addressing of variables, and type casting functions. Most of them are packaged in a module called SYSTEM. These features were supposed to be rarely used and easily visible through the presence of SYSTEM in a module's import list. Experience has revealed, however, that a significant number of programmers import this module quite indiscriminately. A particularly seducing trap are Modula's type transfer functions.

It appears preferable to drop the pretense of portability of programs that import a "standard", yet system-specific module. Both, the module SYSTEM and the *type transfer functions* are therefore eliminated, and with them also the types ADDRESS and WORD. Individual implementations are free to provide system-dependent modules, but they do not belong to the general language definition. Their use then declares a program to be patently implementation-specific, and thereby non-portable.

## Concurrency

The system Oberon does not require any language facilities for expressing concurrent processes. The pertinent, rudimentary features of Modula, in particular the *coroutine*, were

therefore not retained. This exclusion is merely a reflection of our actual needs within the concrete project, but not on the general relevance of concurrency in programming.

## Features introduced in Oberon

### Type extension

The most important addition is the facility of extended record types. It permits the construction of new types on the basis of existing types, and establishes a certain degree of compatibility between the new and old types. Assuming a given type

```
T = RECORD x, y: INTEGER END
```

extensions may be defined which contain certain fields in addition to the existing ones. For example

```
T0 = RECORD (T) z: REAL END
T1 = RECORD (T) w: LONGREAL END
```

define types with fields  $x, y, z$  and  $x, y, w$  respectively. We define a type declared by

```
T' = RECORD (T) <field definitions> END
```

to be a (*direct*) *extension* of  $T$ , and conversely  $T$  to be the (*direct*) *base type* of  $T'$ . Extended types may be extended again, giving rise to the following definitions:

A type  $T'$  is an *extension* of  $T$ , if  $T' = T$  or  $T'$  is a direct extension of an extension of  $T$ . Conversely,  $T$  is a *base type* of  $T'$ , if  $T = T'$  or  $T$  is the direct base type of a base type of  $T'$ . We denote this relationship by  $T' \Rightarrow T$ .

The rule of assignment compatibility states that values of an extended type are assignable to variables of their base types. For example, a record of type  $T0$  can be assigned to a variable of the base type  $T$ . This assignment involves the fields  $x$  and  $y$  only, and in fact constitutes a *projection* of the value onto the space spanned by the base type.

It is important that an extended type may be declared in a module that imports the base type. In fact, this is probably the normal case.

This concept of extensible data type gains importance when extended to pointers. It is appropriate to say that a pointer type  $P'$  bound to  $T'$  extends a pointer type  $P$ , if  $P$  is bound to a base type  $T$  of  $T'$ , and to extend the assignment rule to cover this case. It is now possible to form data structures whose nodes are of different types, i.e. inhomogeneous data structures. The inhomogeneity is automatically (and most sensibly) bounded by the fact that the nodes are linked by pointers of a common base type.

Typically, the pointer fields establishing the structure are contained in the base type  $T$ , and the procedures manipulating the structure are defined in the same (base) module as  $T$ . Individual extensions (variants) are defined in client modules together with procedures operating on nodes of the extended type. This scheme is in full accordance with the notion of system extensibility: new modules defining new extensions may be added to a system without requiring a change of the base modules, not even their recompilation.

As access to an individual node via a pointer bound to a base type provides a projected view of the node data only, a facility to widen the view is necessary. It depends on the

possibility to determine the actual type of the referenced node. This is achieved by a *type test*, a Boolean expression of the form

$$t \text{ IS } T' \quad (\text{or } p \text{ IS } P')$$

If the test is affirmative, an assignment  $t' := t$  ( $t'$  of type  $T'$ ) or  $p' := p$  ( $p'$  of type  $P'$ ) should be possible. The static view of types, however, prohibits this. Note that both assignments violate the rule of assignment compatibility. The desired assignment is made possible by providing a *type guard* of the form

$$t' := t(T') \quad (p' := p(P'))$$

and by the same token access to the field  $z$  of a  $T0$  (see previous examples) is made possible by a type guard in the designator  $t(T0).z$ . Here the guard asserts that  $t$  is (currently) of type  $T0$ .

The declaration of extended record types, the type test, and the type guard are the only additional features introduced in this context. A more extensive discussion is provided in [2]. The concept is very similar to the class notion of Simula 67 [3], Smalltalk [4], and others. Differences lie in the fact that the class facility stipulates that all procedures applicable to objects of the class are defined together with the data definition. It is awkward to be obliged to define a new class solely because a method (procedure) has been added or changed. In Oberon, procedure (method) types rather than methods are connected with objects in the program text. The binding of actual methods (specific procedures) to objects (instances) is delayed until the program is executed. In Smalltalk, the compatibility rules between a class and its subclasses are confined to pointers, thereby intertwining the concepts of access method and data type in an undesirable way. Here, the relationship between a type and its extensions is based on the established mathematical concept of projection.

In Modula, it is possible to declare a pointer type within an implementation module, and to export it as an opaque type by listing the same identifier in the corresponding definition module. The net effect is that the type is exported whereby its associated binding remains hidden (invisible to clients). In Oberon, this facility is generalized in the following way: Let a record type be defined in a certain implementation part, for example

```
Viewer = RECORD width, height: INTEGER; x, y: INTEGER END
```

In the corresponding definition part, a *partial* definition of the same type may be specified, for example

```
Viewer = RECORD width, height: INTEGER END
```

with the effect that a partial view – a *public projection* – is visible to clients. In client modules as well as in the implementation part it is possible to define extensions of the base type (e.g. TextViewers or GraphViewers).

### Type inclusion

Modern processors feature arithmetic operations on several number formats. It is desirable to have all these formats reflected in the language as basic types. Oberon features five of them:

```
LONGINT, INTEGER, SHORTINT (integer types)
LONGREAL, REAL             (real types)
```



With the proliferation of basic types, a relaxation of compatibility rules among them becomes almost mandatory. (Note that in Modula the arithmetic types INTEGER, CARDINAL, and REAL are incompatible). To this end, the notion of type inclusion is introduced: a type T includes a type T', if the values of type T' are also values of type T. Oberon postulates the following hierarchy:

LONGREAL  $\supset$  REAL  $\supset$  LONGINT  $\supset$  INTEGER  $\supset$  SHORTINT

The assignment rule is relaxed accordingly: A value of type T' can be assigned to a variable of type T, if T' is included in T (or if T' extends T), i.e. if  $T \supset T'$  or  $T' \Rightarrow T$ . In this respect, we return to (and extend) the flexibility of Algol 60. For example, given variables

i: INTEGER; k: LONGINT; x: REAL

the assignments

k := i; x := k; x := 1; k := k+i; x := x\*10 + i

are conforming to the rules, whereas the statements  $i := k$ ;  $k := x$  are not acceptable. Finally, it is worth noting that the various arithmetic types represent a limited set of subrange types.

The *multi-dimensional open array* and the *closure statement* (in symmetry to a module's initialization body) are the remaining facilities of Oberon not present in Modula.

## Summary

The language Oberon has evolved from Modula-2 and incorporates the experiences of many years of programming in Modula. A significant number of features have been eliminated. They appear to have contributed more to language and compiler complexity than to genuine power and flexibility of expression. A small number of features have been added, the most significant one being the concept of type extension.

The evolution of a new language that is smaller, yet more powerful than its ancestor is contrary to common practices and trends, but has inestimable advantages. Apart from simpler compilers, it results in a concise defining document [5], an indispensable prerequisite for any tool that must serve in the construction of sophisticated and reliable systems.

## Acknowledgement

It is impossible to explicitly acknowledge all contributions of ideas that ultimately simmered down to what is now Oberon. Most came from the use or study of existing languages, such as Modula-2, Ada, Smalltalk, C++, and Cedar, which often taught us how *not* to do it. Of particular value was the contribution of Oberon's first user, J. Gutknecht. The author is grateful for his insistence on the elimination of deadwood and on basing the remaining features on a sound mathematical foundation.

## References

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# The Programming Language Oberon

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*Make it as simple as possible, but not simpler.*

A. Einstein

## 1. Introduction

Oberon is a general-purpose programming language that evolved from Modula-2. Its principal new feature is the concept of *type extension*. It permits the construction of new data types on the basis of existing ones and to relate them.

This report is not intended as a programmer's tutorial. It is intentionally kept concise. Its function is to serve as a reference for programmers, implementors, and manual writers. What remains unsaid, is mostly left so intentionally, either because it is derivable from stated rules of the language, or because it would require to commit the definition when a general commitment appears as unwise. The moral is: if a specific construct is not defined by the report either directly or derivably, then the programmer should refrain from incorporating it in programs.

## 2. Syntax

A language is an infinite set of sentences, namely the sentences well formed according to its syntax. In Oberon, these sentences are called compilation units. Each unit is a finite sequence of symbols from a finite vocabulary. The vocabulary of Oberon consists of identifiers, numbers, strings, operators, and delimiters. They are called lexical symbols and are composed of sequences of characters. (Note the distinction between symbols and characters.)

To describe the syntax, an extended Backus-Naur Formalism called EBNF is used. Angular brackets [ and ] denote optionality of the enclosed sentential form, and curly brackets { and } denote its repetition (possibly 0 times). Syntactic entities (non-terminal symbols) are denoted by English words expressing their intuitive meaning. Symbols of the language vocabulary (terminal symbols) are strings enclosed in quote marks or words written in capital letters, so-called reserved words. Syntactic rules (productions) are marked by a \$ sign at the left margin of the line.

## 3. Vocabulary and representation

The representation of symbols in terms of characters depends on the underlying character set. The ASCII set is used and the following lexical rules must be observed. Blanks must not occur within symbols (except in strings). Blanks and line breaks are ignored unless they are essential to separate two consecutive symbols. Symbols are identifiers, numbers, strings, operators, and delimiters.

1. *Identifiers* are sequences of letters and digits. The first character must be a letter.

\$ ident = letter {letter | digit}.

Examples:

```
x scan Oberon GetSymbol firstLetter
```

2. *Numbers* are (unsigned) integers or real numbers. Integers are sequences of digits and may be followed by a suffix letter. The type is the minimal type to which the number belongs

(see 6.1.). If no suffix is specified, the representation is decimal. The suffix H indicates hexadecimal representation. The suffix X specifies that the constant is of type CHAR, the hexadecimal value being the character's ordinal number.

A real number always contains a decimal point. Optionally it may also contain a decimal scale factor. The letter E (or D) is pronounced as "times ten to the power of". A real number is of type REAL, unless it has a scale factor containing the letter D; in this case it is of type LONGREAL.

```
$ number = integer | real.
$ integer = digit {digit} | digit {hexDigit} ("H" | "X").
$ real = digit {digit} "." {digit} [ScaleFactor].
$ ScaleFactor = ("E" | "D") ["+" | "-"] digit {digit}.
$ hexDigit = digit | "A" | "B" | "C" | "D" | "E" | "F".
$ digit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9".
```

Examples:

```
1987
100H      = 256
12.3
4.567E8   = 456700000
0.57712566D-6 = 0.00000057712566
```

3. *Character constants* are either denoted by a single character enclosed in quote marks or by the ordinal number of the character in hexadecimal notation followed by the letter X.

4. *Strings* are sequences of characters enclosed in quote marks. Both double quotes and single quotes (apostrophes) may be used as quote marks. However, the opening and closing marks must be the same character, and this character cannot occur within the string. A string must not extend over the end of a line. The number of characters in a string is called the *length* of the string. Strings can be assigned to and compared with arrays of characters (see 9.1 and 8.2.4).

```
$ string = "" {character} "" | ''' {character} '''.
```

Examples:

```
"OBERON" "Don't worry!" 'codeword "Barbarossa"
```

5. *Operators and delimiters* are the special characters, character pairs, or *reserved words* listed below. These reserved words consist exclusively of capital letters and cannot be used in the role of identifiers.

|   |    |            |                |        |
|---|----|------------|----------------|--------|
| + | := | ARRAY      | IMPLEMENTATION | RETURN |
| - | ↑  | BEGIN      | IMPORT         | THEN   |
| * | =  | CASE       | IN             | TO     |
| / | #  | CLOSE      | IS             | TYPE   |
| ~ | <  | CONST      | LOOP           | VAR    |
| & | >  | DEFINITION | MOD            | UNTIL  |
| . | <= | DIV        | NIL            | WITH   |
| , | >= | DO         | OF             | WHILE  |
| ; | .. | ELSE       | OR             |        |
|   | :  | ELSIF      | POINTER        |        |
| ( | )  | END        | PROCEDURE      |        |
| [ | ]  | EXIT       | RECORD         |        |
| { | }  | IF         | REPEAT         |        |

6. *Comments* may be inserted between any two symbols in a program. They are arbitrary character sequences opened by the bracket (\* and closed by \*). Comments do not affect the meaning of a program.

#### 4. Declarations and scope rules

Every identifier occurring in a program must be introduced by a declaration, unless it is a predeclared identifier. Declarations also serve to specify certain permanent properties of an object, such as whether it is a constant, a type, a variable, or a procedure.

The identifier is then used to refer to the associated object. This is possible in those parts of a program only which are within the *scope* of the declaration. The scope extends textually from the point of the declaration to the end of the block (procedure or module) to which the declaration belongs and hence to which the object is *local*. The scope rule is augmented by the following amendments:

1. A type T1 can be used in a declaration of a pointer type T (see 6.7) which textually precedes the declaration of T1, if both T and T1 are declared in the same block.
2. Field identifiers of a record declaration (see 6.3) are valid in field designators only.

An identifier may be *qualified*. In this case it is prefixed by another identifier which designates the module (see Ch. 11) from which the identifier is imported. The prefix and the identifier are separated by a period.

\$ `qualident = [ident "."] ident.`

The following identifiers are predefined; their meaning is defined in the indicated sections:

|         |        |          |        |
|---------|--------|----------|--------|
| ABS     | (10.2) | LONG     | (10.2) |
| ADR     | (10.2) | LONGINT  | (6.1)  |
| ASH     | (10.2) | LONGREAL | (6.1)  |
| BOOLEAN | (6.1)  | LSH      | (10.2) |
| BYTE    | (6.1)  | MAX      | (10.2) |
| CAP     | (10.2) | MIN      | (10.2) |
| CHAR    | (6.1)  | NEW      | (6.4)  |
| CHR     | (10.2) | ODD      | (10.2) |
| DEC     | (10.2) | ORD      | (10.2) |
| ENTIER  | (10.2) | REAL     | (6.1)  |
| EXCL    | (10.2) | ROT      | (10.2) |
| FALSE   | (6.1)  | SET      | (6.1)  |
| HALT    | (10.2) | SHORT    | (10.2) |
| INC     | (10.2) | SHORTINT | (6.1)  |
| INCL    | (10.2) | SIZE     | (10.2) |
| INTEGER | (6.1)  | TRUE     | (6.1)  |
| LEN     | (10.2) |          |        |

#### 5. Constant declarations

A constant declaration associates an identifier with a constant value, i.e. it can be evaluated by a mere textual scan without actually executing the program. Its operands are constants. (see Ch. 8).

\$ `ConstantDeclaration = ident "=" ConstExpression.`

\$ `ConstExpression = expression.`

Examples of constant declarations are

```
N      = 100
limit  = 2*N -1
all    = {0 .. WordSize-1}
```

## 6. Type declarations

A data type determines the set of values which variables of that type may assume and the operators that are applicable, and it associates an identifier with the type. In the case of structured types, it also defines the structure of variables of this type. There are two different structures, namely arrays and records, with different component selectors.

\$ TypeDeclaration = ident "=" type.

\$ type = qualident | ArrayType | RecordType | PointerType | ProcedureType.

Examples:

```
Table      = ARRAY N OF REAL
Tree       = POINTER TO Node
Node       = RECORD key: INTEGER
            left, right: Tree
            END
CenterNode = RECORD (Node)
            name: ARRAY 32 OF CHAR;
            subnode: List
            END
Function    = PROCEDURE (REAL): REAL
```

### 5.1. Basic types

The following basic types are denoted by predeclared identifiers. The associated operators are defined in 8.2, and the predeclared function procedures in 10.2. The values of a given basic type are the following:

1. BOOLEAN the truth values TRUE or FALSE.
2. CHAR the characters of the ASCII set.
3. SHORTINT the integers between MIN(SHORTINT) and MAX(SHORTINT).
4. INTEGER the integers between MIN(INTEGER) and MAX(INTEGER).
5. LONGINT the integers between MIN(LONGINT) and MAX(LONGINT).
6. REAL real numbers between MIN(REAL) and MAX(REAL).
7. LONGREAL real numbers between MIN(LONGREAL) and MAX(LONGREAL).
8. SET the sets of integers between 0 and MAX(SET).
9. BYTE this type includes CHAR and SHORTINT.

Types 3 to 5 are *integer* types, 6 and 7 are *real* types, and together they are called *numeric* types. They form a hierarchy; the larger type *includes* (the values of) the smaller type:

LONGREAL  $\supset$  REAL  $\supset$  LONGINT  $\supset$  INTEGER  $\supset$  SHORTINT

### 6.2. Array types

An array is a structure consisting of a fixed number of elements which are all of the same type, called the *element type*. The number of elements of an array is called its *length*. The elements of the array are designated by indices, which are integers between 0 and the length minus 1.

```
$ ArrayType = ARRAY length {"," length} OF type.
$ length = ConstExpression.
```

A declaration of the form

```
ARRAY N0, N1, ..., Nk OF T
```

is understood as an abbreviation of the declaration

```
ARRAY N0 OF
  ARRAY N1 OF
    ...
    ARRAY Nk OF T
```

Examples of array types:

```
ARRAY N OF INTEGER
ARRAY 10, 20 OF REAL
```

### 6.3. Record types

A record type is a structure consisting of a fixed number of elements of possibly different types. The record type declaration specifies for each element, called *field*, its type and an identifier which denotes the field. The scope of these field identifiers is the record definition itself, but they are also visible within field designators (see 8.1) referring to elements of record variables.

```
$ RecordType = RECORD [{" BaseType "} ] FieldListSequence END.
$ BaseType = qualident.
$ FieldListSequence = FieldList {";" FieldList}.
$ FieldList = [IdentList ":" type].
$ IdentList = ident {"," ident}.
```

Record types are extensible, i.e. a record type can be defined as an extension of another record type. In the examples above, *CenterNode* (*directly*) *extends* *Node*, which is the (*direct*) *base type* of *CenterNode*. More specifically, *CenterNode* extends *Node* with the fields *name* and *subnode*.

*Definition:* A type *T0* *extends* a type *T*, if it equals *T*, or if it directly extends an extension of *T*. Conversely, a type *T* is a *base type* of *T0*, if it equals *T0*, or if it is the direct base type of a base type of *T0*.

Examples of record types:

```
RECORD day, month, year: INTEGER
END
RECORD
  name, firstname: ARRAY 32 OF CHAR;
  age: INTEGER;
  salary: REAL
END
```

### 6.4. Pointer types

Variables of a pointer type *P* assume as values pointers to variables of some record type *T*. These variables are dynamically allocated by explicit execution of a statement. The pointer type *P* is said to be *bound* to *T*.

\$ PointerType = POINTER TO type.

If  $p$  is a variable of type  $P = \text{POINTER TO } T$ , then a call of the predeclared procedure  $\text{NEW}(p)$  has the following effect (see 10.2): A variable of type  $T$  is allocated in free storage, and a pointer to it is assigned to  $p$ . This pointer  $p$  is of type  $P$ ; the *referenced* variable  $p\uparrow$  is of type  $T$ . Every pointer variable may assume the value  $\text{NIL}$ , which points to no variable at all.

## 6.5. Procedure types

Variables of a procedure type  $T$  have a procedure as value. If a procedure  $P$  is assigned to a procedure variable of type  $T$ , the (types of the) formal parameters of  $P$  must be the same as those indicated in the formal type list of  $T$ . The same holds for the result type in the case of a function procedure.

Restriction:  $P$  must not be declared local to another procedure, and neither can it be a predeclared procedure.

\$ ProcedureType = PROCEDURE [FormalTypeList].

\$ FormalTypeList = "(" ([VAR] FormalType {"," [VAR] FormalType}) ")" [":"qualident].

## 7. Variable declarations

Variable declarations serve to introduce variables and associate them with a unique identifier and a fixed data type. Variables whose identifiers appear in the same list all obtain the same type.

\$ VariableDeclaration = IdentList ":" type.

Examples of variable declarations (refer to examples in Ch. 6):

```

i, j:   INTEGER
x:      REAL
p, q:   BOOLEAN
s:      SET
F:      Function
a:      ARRAY 100 OF REAL
w:      ARRAY 16 OF
        RECORD ch: CHAR;
        count: INTEGER
        END
t:      Tree

```

## 8. Expressions

Expressions are constructs denoting rules of computation for obtaining values of variables and constants, and for generating new values by the application of operators and function procedures. Expressions consist of operands and operators. Parentheses may be used to express specific associations of operators and operands.

### 8.1. Operands

With the exception of literal constants, i.e. numbers, character strings, and sets (see Ch. 5), operands are denoted by *designators*. A designator consists of an identifier referring to the constant, variable, or procedure to be designated. This identifier may possibly be qualified by



module identifiers (see Ch. 4 and 11), and it may be followed by selectors, if the designated object is an element of a structure.

If  $A$  designates an array, then  $A[E]$  denotes that element of  $A$  whose index is the current value of the expression  $E$ . The type of  $E$  must be an integer type. A designator of the form  $A[E_1, E_2, \dots, E_n]$  stands for  $A[E_1][E_2] \dots [E_n]$ . If  $p$  designates a pointer variable,  $p^*$  denotes the variable which is referenced by  $p$ . If  $r$  designates a record, then  $r.f$  denotes the field  $f$  of  $r$ , and if  $p$  designates a pointer,  $p.f$  denotes the field  $f$  of the record  $p^*$ , i.e. the dot implies dereferencing and  $p.f$  stands for  $p^*.f$ .

The *typeguard*  $v(T)$  asserts that  $v$  is of type  $T$  (see Ch. 6). It is applicable, if  $v$  refers to a variable indirectly and if the declared type of  $v$  includes the actual record type  $T$  of the referenced variable. Indirect reference is implied, if  $v$  is a pointer, or if  $v$  is a variable parameter.

```
$ designator = qualident {"." ident | "[" ExpList "]" | "(" qualident ")" | "↑" }.
$ ExpList = expression {"." expression}.
```

If the designated object is a variable, then the designator refers to the variable's current value. If the object is a procedure, a designator without parameter list refers to that procedure. If it is followed by a (possibly empty) parameter list, the designator implies an activation of the procedure and stands for the value resulting from its execution. The (types of these) actual parameters must correspond to the formal parameters as specified in the procedure's declaration (see Ch. 10).

Examples of designators (see examples in Ch. 7):

```
i                (INTEGER)
a[i]             (REAL)
w[3].ch         (CHAR)
t.key           (INTEGER)
t.left.right    (TreePtr)
t(CenterNode).subnode (ListPtr)
```

## 8.2. Operators

The syntax of expressions distinguishes between four classes of operators with different precedences (binding strengths). The operator  $\sim$  has the highest precedence, followed by multiplication operators, addition operators, and relations. Operators of the same precedence associate from left to right. For example,  $x-y-z$  stands for  $(x-y)-z$ .

```
$ expression = SimpleExpression [relation SimpleExpression].
$ relation = "=" | "#" | "<" | "<=" | ">" | ">=" | IN | IS.
$ SimpleExpression = ["+" | "-" ] term {AddOperator term}.
$ AddOperator = "+" | "-" | OR .
$ term = factor {MulOperator factor}.
$ MulOperator = "*" | "/" | DIV | MOD | "&".
$ factor = number | string | NIL | set | designator [ActualParameters] |
  "(" expression ")" | "-" factor.
$ set = "{" [element {"." element}] "}".
$ element = expression [{".." expression}].
$ ActualParameters = "(" [ExpList] ")" .
```

The available operators are listed in the following tables. In some instances, several different operations are designated by the same operator symbol. In these cases, the actual operation is identified by the type of the operands. Further operations are available through standard functions (see 10.2.).

### 8.2.1. Logical operators

| <u>symbol</u> | <u>result</u>       |
|---------------|---------------------|
| OR            | logical disjunction |
| &             | logical conjunction |
| ~             | negation            |

These operators apply to BOOLEAN operands and yield a BOOLEAN result.

|        |   |
|--------|---|
| p OR q | stands for "if p then TRUE, otherwise q"  |
| p & q  | stands for "if p then q, otherwise FALSE" |
| ~ p    | stands for "not p"                        |

### 8.2.2. Arithmetic operators

| <u>symbol</u> | <u>result</u>    |
|---------------|------------------|
| +             | sum              |
| -             | difference       |
| *             | product          |
| /             | quotient         |
| DIV           | integer quotient |
| MOD           | modulus          |

The operators +, -, \*, and / apply to operands of arithmetic types. The type of the result is that operand's type which includes the other operand's type, except for division (/), where the result is the real type which includes both operand types. When used as operators with a single operand, - denotes sign inversion and + denotes the identity operation.

The operators DIV and MOD apply to integer operands only. The operators DIV and MOD are related by the following formulas defined for  $y > 0$ :

$$x = (x \text{ DIV } y) * y + (x \text{ MOD } y) \quad 0 \leq (x \text{ MOD } y) < y$$

### 8.2.3. Set operators

| <u>symbol</u> | <u>result</u>            |
|---------------|--------------------------|
| +             | union                    |
| -             | difference               |
| *             | intersection             |
| /             | symmetric set difference |

The monadic minus sign denotes the complement of x, i.e. -x denotes the set of integers between 0 and MAX(SET) which are not in x.

$$\begin{aligned} x - y &= x * (-y) \\ x / y &= (x - y) + (y - x) \end{aligned}$$

### 8.2.4. Relations

| <u>symbol</u> | <u>relation</u>  |
|---------------|------------------|
| =             | equal            |
| #             | unequal          |
| <             | less             |
| <=            | less or equal    |
| >             | greater          |
| >=            | greater or equal |
| IN            | set membership   |
| IS            | type test        |

Relations are Boolean. The ordering relations apply to the numeric types, CHAR, and character arrays (strings). The relations = and # also apply to sets, pointers, and procedure types.

$x \text{ IN } s$  stands for "x is an element of s". x must be of an integer type, and s of type SET.

$v \text{ IS } T$  stands for "v is of type T" and is called a *type test*. It is applicable, if v refers to a variable indirectly and the declared type of v includes the actual record type T of the referenced variable. Assuming, for instance, that T includes T1 and that v is a designator declared of type T, then the test "v IS T1" determines whether the actually designated variable is (not only a T, but also) a T1.

Examples of expressions (refer to examples in Ch. 7):

```

1987          (INTEGER)
i DIV 3       (INTEGER)
~p OR q       (BOOLEAN)
(i+j) * (i-j) (INTEGER)
s - {8, 9, 13} (SET)
i + x         (REAL)
a[i+j] * a[i-j] (REAL)
(0<=i) & (i<100) (BOOLEAN)
t.key = 0     (BOOLEAN)
k IN {i ..j-1} (BOOLEAN)
v IS CenterNode (BOOLEAN)

```

## 9. Statements

Statements denote actions. There are elementary and structured statements. Elementary statements are not composed of any parts that are themselves statements. They are the assignment, the procedure call, and the return and exit statements. Structured statements are composed of parts that are themselves statements. They are used to express sequencing and conditional, selective, and repetitive execution. A statement may also be empty, in which case it denotes no action. The empty statement is included in order to relax punctuation rules in statement sequences.

```

$ statement = [assignment | ProcedureCall |
$           IfStatement | CaseStatement | WhileStatement | RepeatStatement |
$           LoopStatement | WithStatement | EXIT | RETURN [expression] ].

```

### 9.1. Assignments

The assignment serves to replace the current value of a variable by a new value specified by an expression. The assignment operator is written as " := " and pronounced as *becomes*.

```
$ assignment = designator " := " expression.
```

The type of the expression must be included by, or it must extend the type of the variable. The following exceptions hold:

1. The constant NIL can be assigned to variables of any pointer type.
2. Strings can be assigned to any variable whose type is an array of characters, provided the length of the string is less than that of the array. If a string s of length n is assigned to an array a, the result is  $a[i] = s[i]$  for  $i = 0 \dots n-1$ , and  $a[n] = 0X$ .
3. Values designated as public parts cannot be assigned (see Ch. 11).

Examples of assignments (see examples in Ch. 7):

```

i := 0
p := i = j
x := i + 1
j := log2(i+j)
F := log2
s := {2, 3, 5, 7, 11, 13}
a[i] := (x+y) * (x-y)
t.key := i
w[i+1].ch := "A"

```

## 9.2. Procedure calls

A procedure call serves to activate a procedure. The procedure call may contain a list of actual parameters which are substituted in place of their corresponding formal parameters defined in the procedure declaration (see Ch. 10). The correspondence is established by the positions of the parameters in the lists of actual and formal parameters respectively. There exist two kinds of parameters: *variable* and *value parameters*.

In the case of variable parameters, the actual parameter must be a designator denoting a variable. If it designates an element of a structured variable, the selector is evaluated when the formal/actual parameter substitution takes place, i.e. before the execution of the procedure. If the parameter is a value parameter, the corresponding actual parameter must be an expression. This expression is evaluated prior to the procedure activation, and the resulting value is assigned to the formal parameter which now constitutes a local variable. The types of corresponding actual and formal parameters must be identical in the case of variable parameters and comply with the rule of assignment in the case of value parameters (see 9.1.). Exception are specified in 10.1.

\$ ProcedureCall = designator [ActualParameters].

Examples of procedure calls:

```

ReadInt(i)      (see Ch. 10)
WriteInt(j*2+1, 6)
INC(a[i])

```

## 9.3. Statement sequences

Statement sequences denote the sequence of actions specified by the component statements which are separated by semicolons.

\$ StatementSequence = statement {";" statement}.

## 9.4. If statements

```

$ IfStatement =   IF expression THEN StatementSequence
$                 {ELSIF expression THEN StatementSequence}
$                 [ELSE StatementSequence]
$                 END.

```

If statements specify the conditional execution of guarded statements. The Boolean expression preceding a statement is called its *guard*. The guards are evaluated in sequence of occurrence, until one evaluates to TRUE, whereafter its associated statement sequence is executed. If no guard is satisfied, the statement sequence following the symbol ELSE is executed, if there is one.

Example:

```

IF (ch >= "A") & (ch <= "Z") THEN ReadIdentifier
ELSIF (ch >= "0") & (ch <= "9") THEN ReadNumber
ELSIF ch = "" THEN ReadString("")
ELSIF ch = " " THEN ReadString(" ")
ELSE SpecialCharacter
END

```

## 9.5. Case statements

Case statements specify the selection and execution of a statement sequence according to the value of an expression. First the case expression is evaluated, then the statement sequence is executed whose case label list contains the obtained value. The type of the case expression must be an integer type or CHAR, and all labels must be of that type. Case labels are constants, and no value must occur more than once. If the value of the expression does not occur as a label of any case, the statement sequence following the symbol ELSE is selected, if there is one. Otherwise it is considered as an error.

```

$ CaseStatement = CASE expression OF case
$               {"|" case}
$               [ELSE StatementSequence]
$               END.
$ case =        [CaseLabelList ":" StatementSequence].
$ CaseLabelList = CaseLabels {"|" CaseLabels}.
$ CaseLabels =  ConstExpression [".." ConstExpression].

```

Example:

```

CASE ch OF
  "A" .. "Z": ReadIdentifier
| "0" .. "9": ReadNumber
| " ":      ReadString
| " ":      ReadString
ELSE       SpecialCharacter
END

```

Note: Case statements are used when the case labels form a (nearly) contiguous set of values.

## 9.6. While statements

While statements specify the repeated execution of guarded statements (see 9.4.). The guards are evaluated in sequence of occurrence, until one evaluates to TRUE, whereafter its associated statement sequence is executed. Then this process is repeated. The repetition stops when all guards yield the value FALSE.

```

$ WhileStatement = WHILE expression DO StatementSequence
$               {ELSIF expression DO StatementSequence}
$               END.

```

Examples:

```

WHILE j > 0 DO
  j := j DIV 2; i := i+1
END
WHILE j < i DO i := i-j
ELSIF i < j DO j := j-i
END

```

```

WHILE (t # NIL) & (t.key # i) DO
  t := t.left
END

```

### 9.7. Repeat Statements

A repeat statement specifies the repeated execution of a statement sequence until a condition is satisfied. The statement sequence is executed at least once.

```
$ RepeatStatement = REPEAT StatementSequence UNTIL expression.
```

### 9.8. Loop statements

A loop statement specifies the repeated execution of a statement sequence. It is terminated by the execution of any exit statement within that sequence.

```
$ LoopStatement = LOOP StatementSequence END.
```

Example:

```

LOOP
  IF t1 = NIL THEN EXIT END ;
  IF x < t1.key THEN t2 := t1.left; p := TRUE
  ELSIF x > t1.key THEN t2 := t1.right; p := FALSE
  ELSE EXIT
  END ;
  t1 := t2
END

```

While and repeat statements can be expressed by loop statements containing a single exit statement. Their use is recommended as they characterize the most frequently occurring situations where termination depends either on a single condition at either the beginning or end of the repeated statement sequence. The loop statement is useful to express cases with several termination conditions and points. Exit statements are contextually, although not syntactically bound to the loop statement which contains them (see 9.9.).

### 9.9. Return and exit statements

A return statement consists of the symbol RETURN, possibly followed by an expression. It indicates the termination of a procedure, and the expression specifies the result of a function procedure. Its type must be identical to the result type specified in the procedure heading (see Ch. 10).

Function procedures require the presence of a return statement indicating the result value. There may be several, although only one will be executed. In proper procedures, a return statement is implied by the end of the procedure body. An explicit return statement therefore appears as an additional, probably exceptional termination point.

An exit statement consists of the symbol EXIT, and it specifies termination of the enclosing loop statement and continuation with the statement following that loop statement (see 9.8).

### 9.10. With statements

If a pointer variable or a variable parameter with record structure is of a base type T, it may be designated in the heading of a with clause together with a type T0 included in T. Then this variable is treated within the with statement as if it had been declared of type T0. The

with statement assumes a role similar to the type guard, extending the guard over an entire statement sequence. It may be regarded as a *regional* type guard.

```
$ WithStatement = WITH qualident ":" qualident DO StatementSequence END .
```

Example:

```
WITH v: CenterNode DO name := v.name; L := v.subnode END
```

## 10. Procedure declarations

Procedure declarations consist of a *procedure heading* and a block which is said to be the *procedure body*. The heading specifies the procedure identifier, the *formal parameters*, and the result type (if any). The block contains declarations and statements. The procedure identifier is repeated at the end of the procedure declaration.

There are two kinds of procedures, namely *proper procedures* and *function procedures*. The latter are activated by a function designator as a constituent of an expression, and yield a result that is an operand in the expression. Proper procedures are activated by a procedure call. The function procedure is distinguished in the declaration by indication of the type of its result following the parameter list. Its body must contain a RETURN statement which defines the result of the function procedure.

All constants, variables, types, and procedures declared within the block that constitutes the procedure body are *local* to the procedure. The values of local variables are undefined upon entry to the procedure. Since procedures may be declared as local objects too, procedure declarations may be nested. Every object is said to be declared at a certain *level* of nesting. If it is declared local to a procedure at level  $k$ , it has itself level  $k+1$ . Objects declared not within another procedure are defined to be at level 0.

In addition to its formal parameters and local objects, also the objects declared in the environment of the procedure are known and accessible in the procedure (with the exception of those objects that have the same name as an object declared locally).

The use of the procedure identifier in a call within its declaration implies recursive activation of the procedure.

```
$ ProcedureDeclaration = ProcedureHeading ";" ProcedureBody ident.
$ ProcedureHeading = PROCEDURE ["*"] ident [FormalParameters].
$ ProcedureBody = DeclarationSequence [BEGIN StatementSequence] END.
$ ForwardDeclaration = PROCEDURE "^" ident [FormalParameters].
$ DeclarationSequence = [CONST {ConstantDeclaration ";"}]
$ [TYPE {TypeDeclaration ";"}] [VAR {VariableDeclaration ";"}]
$ {ProcedureDeclaration ";" | ForwardDeclaration ";"}
```

A *forward declaration* serves to allow forward references to a procedure that appears later in the text in full. The actual declaration – which specifies the body – must indicate the same parameters and result type (if any) as the forward declaration, and it must be within the same scope. An asterisk following the symbol PROCEDURE is a hint to the compiler and specifies that the procedure is to be usable as parameter and assignable to variables of a compatible procedure type.

### 10.1. Formal parameters

Formal parameters are identifiers which denote actual parameters specified in the procedure call. The correspondence between formal and actual parameters is established when the procedure is called. There are two kinds of parameters, namely *value* and *variable parameters*. The kind is indicated in the formal parameter list. Value parameters stand for local variables to which the result of the evaluation of the corresponding actual parameter is

assigned as initial value. Variable parameters correspond to actual parameters that are variables, and they stand for these variables. Variable parameters are indicated by the symbol VAR, value parameters by the absence of the symbol VAR.

Formal parameters are local to the procedure, i.e. their scope is the program text which constitutes the procedure declaration.

```
$ FormalParameters = "(" [FPSection {";" FPSection}] ")" [":" qualident].
$ FPSection = [VAR] IdentList ":" FormalType.
$ FormalType = {ARRAY OF} qualident.
```

The type of each formal parameter is specified in the parameter list. For variable parameters, it must be a base type of the type of the corresponding actual parameter. For value parameters, the rule of assignment holds (see 9.1), except if the parameter is an *open array*: if a parameter's type is specified as

ARRAY OF T

the parameter is said to be an *open array parameter*. Its type can be considered as the base type of all arrays with the same element type. The formal array can be accessed elementwise only, or it may occur as actual parameter corresponding to a formal parameter which is also an open array.

In the case of a variable parameter with formal type BYTE, the corresponding actual parameter may be of type CHAR or SHORTINT. If the formal type is ARRAY OF BYTE, any actual parameter type is permitted.

A function procedure without parameters has an empty parameter list. It must be called by a function designator whose actual parameter list is empty too.

Restrictions: If a formal parameter specifies a procedure type, then the corresponding actual parameter must be either a procedure declared at level 0 or a variable (or parameter) of that procedure type. It cannot be a predefined procedure.

The result type of a procedure can be neither a record nor an array.

Examples of procedure declarations:

```
PROCEDURE ReadInt(VAR x: INTEGER);
  VAR i: INTEGER; ch: CHAR;
BEGIN i := 0; Read(ch);
  WHILE ("0" <= ch) & (ch <= "9") DO
    i := 10*i + (ORD(ch)-ORD("0")); Read(ch)
  END ;
  x := i
END ReadInt

PROCEDURE WriteInt(x, n: INTEGER); (* 0 <= x < 10^5 *)
  VAR i: INTEGER;
  buf: ARRAY 5 OF INTEGER;
BEGIN i := 0;
  REPEAT buf[i] := x MOD 10; x := x DIV 10; INC(i) UNTIL x = 0;
  WHILE n > i DO Write(" "); DEC(n) END ;
  REPEAT DEC(i); Write(CHR(buf[i] + ORD("0"))) UNTIL i = 0
END WriteInt

PROCEDURE log2(x: INTEGER): INTEGER;
  VAR y: INTEGER; (*assume x>0*)
BEGIN y := 0;
  WHILE x > 1 DO x := x DIV 2; INC(y) END ;
```



RETURN y  
END log2

## 10.2. Predefined procedures

The following table lists the predefined procedures. Some are *generic* procedures, i.e. they apply to several types of operands. *v* stands for a variable, *x* and *n* for expressions, and *T* for a type.

Function procedures:

| Name      | Argument type           | Result type | Function                                     |
|-----------|-------------------------|-------------|--|
| ABS(x)    | numeric type            | type of x   | absolute value                               |
| ODD(x)    | integer type            | BOOLEAN     | $x \text{ MOD } 2 = 1$                       |
| CAP(x)    | CHAR                    | CHAR        | corresponding capital letter                 |
| ASH(x, n) | x, n: integer type      | type of x   | arithmetic shift                             |
| LSH(x, n) | x: SET n: integer type  | SET         | logical shift                                |
| ROT(x, n) | x: SET; n: integer type | SET         | rotation                                     |
| LEN(v, n) | open array              | INTEGER     | the length of <i>v</i> in dimension <i>n</i> |
| ADR(v)    | any                     | LONGINT     | address of variable <i>v</i>                 |
| SIZE(T)   | any                     | INTEGER     | number of bytes required by <i>T</i>         |
| MAX(T)    | T = basic type          | T           | maximum value of type <i>T</i>               |
| MIN(T)    | T = basic type          | T           | minimum value of type <i>T</i>               |

$$\text{ASH}(x, n) = x * 2^n$$

$$\text{LSH}(x, n) = \{i : 0 \leq i < N : (i-n) \text{ IN } s\} \quad \text{where } N = \text{MAX}(\text{SET}) + 1$$

$$\text{ROT}(x, n) = \{i : 0 \leq i < N : (i-n) \text{ MOD } N \text{ IN } s\}$$

Type conversion procedures:

| Name      | Argument type                  | Result type                    | Function                                  |
|-----------|--------------------------------|--------------------------------|---|
| ORD(x)    | CHAR, BYTE                     | INTEGER                        | ordinal number of <i>x</i>                |
| CHR(x)    | integer type, BYTE             | CHAR                           | character with ordinal number <i>x</i>    |
| SHORT(x)  | LONGINT<br>INTEGER<br>LONGREAL | INTEGER<br>SHORTINT<br>REAL    | identity                                  |
| LONG(x)   | SHORTINT<br>INTEGER<br>REAL    | INTEGER<br>LONGINT<br>LONGREAL | identity                                  |
| ENTIER(x) | real type                      | LONGINT                        | largest integer not greater than <i>x</i> |

Note that  $\text{ENTIER}(i/j) = i \text{ DIV } j$

Proper procedures:

| Name   | Argument types | Function   |
|--------|----------------|------------|
| INC(v) | integer type   | $v := v+1$ |
| DEC(v) | integer type   | $v := v-1$ |

|            |                         |                             |
|------------|-------------------------|-----------------------------|
| INCL(v, x) | v: SET; x: integer type | v := v + {x}                |
| EXCL(v, x) | v: SET; x: integer type | v := v - {x}                |
| NEW(v)     | pointer type            | allocate v†                 |
| HALT(x)    | integer constant        | terminate program execution |

In HALT(x), x is a parameter whose interpretation is left to the underlying system implementation.

## 11. Modules

A module constitutes a collection of declarations of constants, types, variables, and procedures, and a sequence of statements for the purpose of initializing the variables. A module consists of two textually separate parts, the *definition part* and the *implementation part*. Both parts are accepted by compilers as *compilation units*.

The *definition part* specifies the names and properties of objects that are relevant to clients, i.e. to other modules which import the module to make use of its facilities.

The *implementation part* contains local objects and statements that need not be visible in client modules and remain hidden. Typically, the definition part contains constant and type declarations, and specifications of procedure headings. The corresponding implementation part contains the complete procedure declarations, and possibly further declarations of objects that remain invisible outside the module.

Definition and implementation parts exist in pairs. Both may contain an import list of modules to be referenced. All objects declared in the definition part are available in the corresponding implementation part. Imports are module identifiers. The form " $M : M_0$ " serves to associate with the identifier  $M$  a module with external name  $M_0$ .

```

$ DefinitionPart = DEFINITION ident ";" [ImportList] DefinitionSequence END ident "." .
$ ImportList = IMPORT import {"," import} ";" .
$ import = ident [":" ident].
$ DefinitionSequence = [CONST {ConstantDeclaration ";"}]
$ [TYPE {TypeDeclaration ";"}] [VAR {VariableDeclaration ";"}]
$ {ProcedureHeading ";"}.
$ ImplementationPart = IMPLEMENTATION ident ";" [ImportList] DeclarationSequence
$ [BEGIN StatementSequence] [CLOSE StatementSequence] END ident "." .
$ CompilationUnit = DefinitionPart | ImplementationPart.
```

The statement sequence following the symbol BEGIN is executed when the module is loaded, i.e. it serves as an initialization command. The statement sequence following the symbol CLOSE is executed when the module is discharged from a system, i.e. made unavailable.

A record type declared in a definition part may be extended in the corresponding definition part by an extended re-declaration. The former is then called the *public part* of the whole. Only the fields defined in the public part are visible to client modules; the other ones remain hidden from clients. The visible fields must be declared preceding the hidden ones, and occur with the same identifiers and types and in the same sequence in both definition and implementation parts.

Example: in definition part:

```
TYPE Viewer = RECORD width, height: INTEGER END
```

in implementation part:

```
TYPE Viewer = RECORD width, height, x, y: INTEGER;  
                  next: ViewerPtr; obj: ObjPtr  
                END
```